

Linear Inequalities Lesson 2 (With text assignment)

Chapter 5 – Systems of Linear Inequalities

Section 5.3 Graphing to Solve Systems of Linear Inequalities

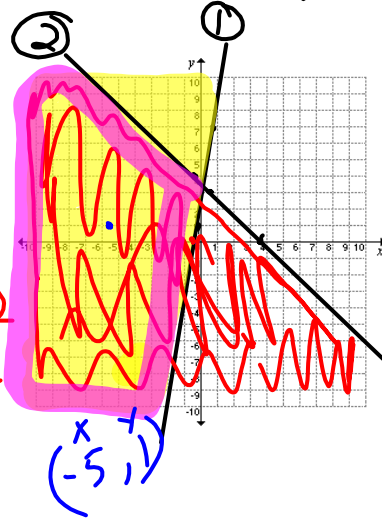
RF1: Model and solve problems that involve systems of linear inequalities in two variables.

For a system of linear equations, the solution is the point where the two lines intersect. (NRF10)
 For a system of linear inequalities, the solution is where the shading for each inequality overlaps.

Example 1: Solve the systems of inequalities by graphing.

① $y \geq 6x + 1$
 ② $x + y \leq 4$

① (0,0) Test
 $0 \geq 6(0) + 1$
 $0 \geq 1$ ✗



What are two possible solutions to this system? Prove one of them.

② $x + y \leq 4 - x$ Test (0,0)
 $0 + 0 \leq 4$
 $0 \leq 4$ ✓

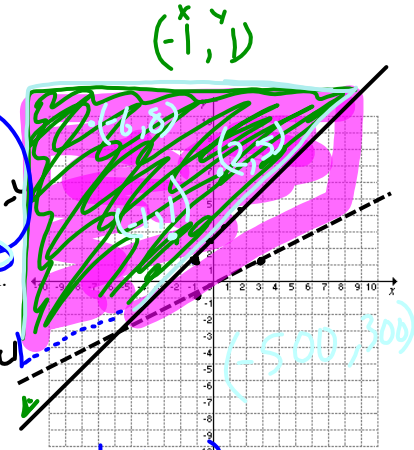
① $1 \geq 6(-5) + 1$
 $1 \geq -30 + 1$
 $1 \geq -29$ ✓

② $(-5) + (1) \leq 4$
 $-4 \leq 4$ ✓

$y = \frac{1}{6}x + \frac{1}{6}$

1) $y \geq x$
 2) $x + 2y > -4$

$y > \frac{1}{2}x - 4$
 $y > \frac{1}{2}x - 4$



What are two possible solutions to this system? Prove one of them.

② $-x + 2y = -4$

$y \text{ int } (x=0)$
 $-x + 2y = -4$
 $0 + 2y = -4$
 $\frac{2y}{2} = \frac{-4}{2}$
 $y = -2$

$x \text{ int } (y=0)$
 $-x + 2(0) = -4$
 $-x = -4$
 $\frac{-x}{-1} = \frac{-4}{-1}$
 $x = 4$ Test (0,0)
 $0 + 0 > -4$
 $0 > -4$ ✓

Test (-1, 1)
 $y \geq x$
 $1 \geq -1$ ✓

Verify (2, 5)
 ① $y \geq x$
 $(5) \geq (2)$ ✓
 ② $-x + 2y > -4$
 $-(2) + 2(5) > -4$
 $-2 + 10 > -4$
 $8 > -4$ ✓

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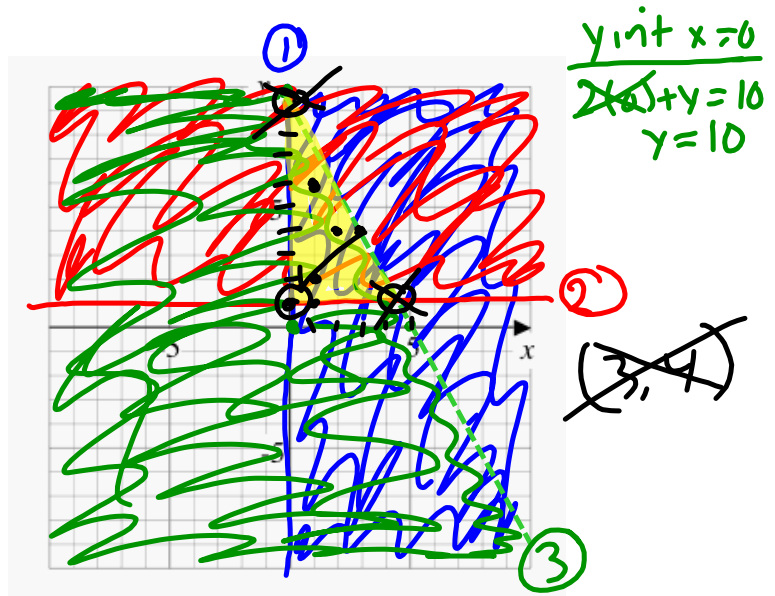
Graph the region defined by these inequalities:

① $x \geq 0$

② $y \geq 1$

③ $2x + y < 10$

$$\begin{aligned} & \text{y int } (y=0) \\ & \frac{2x + (0) = 10}{2} \\ & \boxed{x = 5} \end{aligned}$$



What are three solutions to this system?

$(1, 2)$

$(0, 1)$

$(1, 1)$

$(2, 3)$

Is the point of intersection part of the solution set?

✓

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Graph the following system.

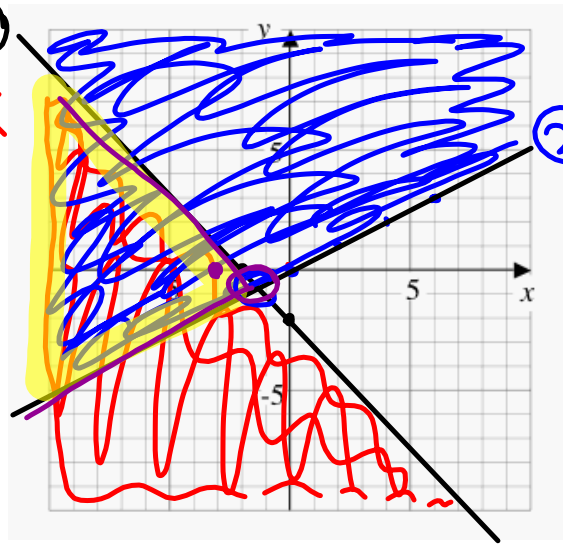
$$\textcircled{1} (x, y) \mid x + y \leq -2, x \in \mathbb{I}, y \in \mathbb{I}$$

$$\textcircled{2} (x, y) \mid 2y \geq x, x \in \mathbb{I}, y \in \mathbb{I}$$

$x \text{ int}$	$y \text{ int}$
$y = -2$	$y = -2$

$$2y \geq x \quad y = \frac{1}{2}x$$

$$\frac{2y}{2} = \frac{1x}{2}$$



a) Give one solution and verify it.

$$\boxed{(-3, 0)}$$

$$\textcircled{1} \begin{aligned} x + y &\leq -2 \\ (-3) + (0) &\leq -2 \\ \boxed{-3 \leq -2} &\quad \checkmark \end{aligned}$$

$$\textcircled{2} \begin{aligned} 2y &\geq x \\ 2(0) &\geq -3 \\ \boxed{0 \geq -3} &\quad \checkmark \end{aligned}$$

b) Are the boundary lines and point of intersection part of the solution set?

Linear Inequalities Lesson 2 (With text assignment)

To raise funds to buy new instruments, the band committee has 500 t-shirts to sell. The shirts come in red or blue. Based on sales of the same t-shirts at a fundraiser last year, the committee expects to sell at least twice as many blue t-shirts as red t-shirts.

x - Red
y - blue

$$\textcircled{1} x + y \leq 500 \rightarrow y \leq -\frac{1}{1}x + 500$$

$$\textcircled{2} 2x \leq y$$

a. Define the variables and restrictions. Write a system of linear inequalities that models the situation.

$$x + y \leq 500 \quad \text{and} \quad y \geq 2x$$

$$\{x, y \mid x + y \leq 500, x \in W, y \in W\}$$

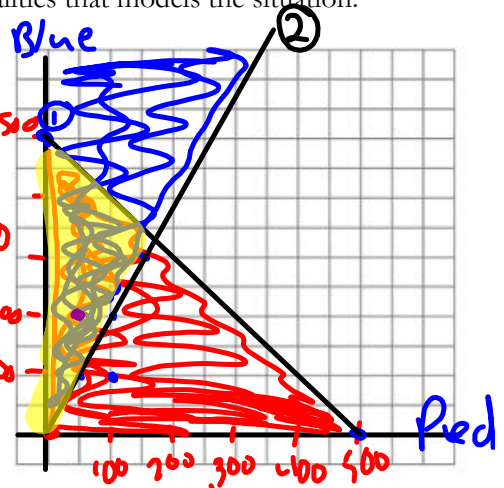
$$\{x, y \mid y \geq 2x, x \in W, y \in W\}$$

b. Graph the system of inequalities.

$$\textcircled{2} \frac{2x \leq y}{y = \frac{1}{2}x + 0}$$

$$\textcircled{1} \frac{x \text{ int}}{x = 500}$$

$$\frac{y \text{ int}}{y = 500}$$



c. Suggest a combination of t-shirt sales that could be made.

$$\textcircled{2} \text{Test}(100, 100)$$

$$2x \leq y$$

$$2(100) \leq 100$$

$$200 \leq 100 \quad \times$$

$$\textcircled{1} \text{Test}(0, 0)$$

$$x + y \leq 500$$

$$0 + 0 \leq 500$$

$$0 \leq 500 \quad \checkmark$$

Solution
(50, 200)
red blue

50 red and 200 blue.

Linear Inequalities Lesson 2 (With text assignment)

Assignment Pg. 235-7 #2, 4 bd, and 8

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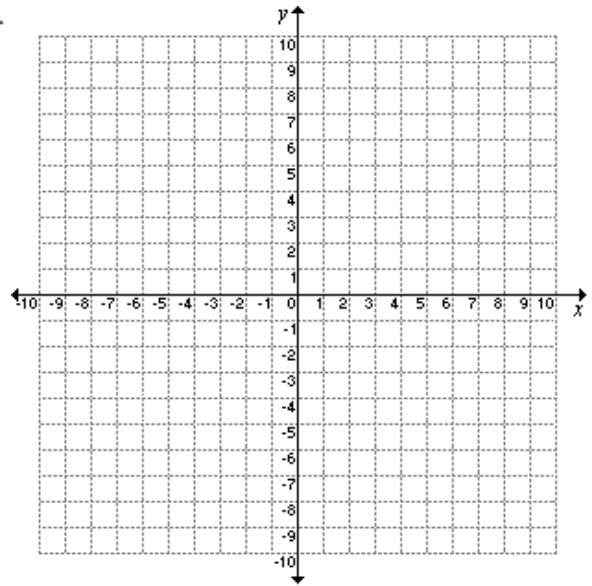
2. a) Graph the solution set for this system of inequalities. Determine a solution. Check its validity. Describe the solution region.

$$x \leq 6$$

$$3y - x < 6$$

- b) Determine if each point is in the solution region.

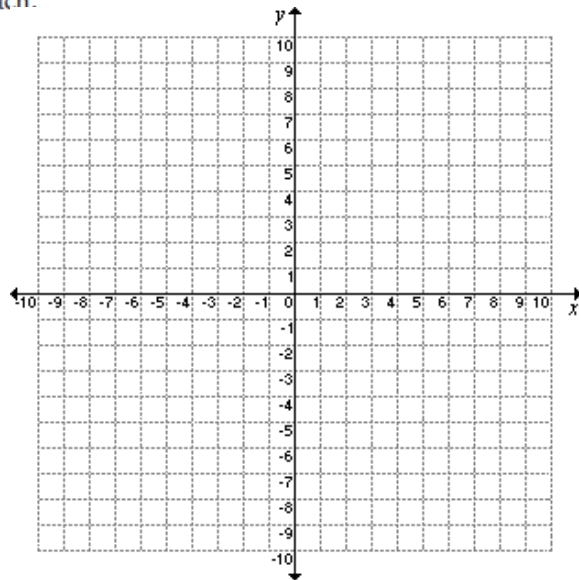
i) (6, 4) ii) (8, 2) iii) (3, 2) iv) (3, 3)



4. Graph each system. Determine a solution for each.

b) $\{(x, y) \mid 2x + y > 0, x \in \mathbb{W}, y \in \mathbb{W}\}$

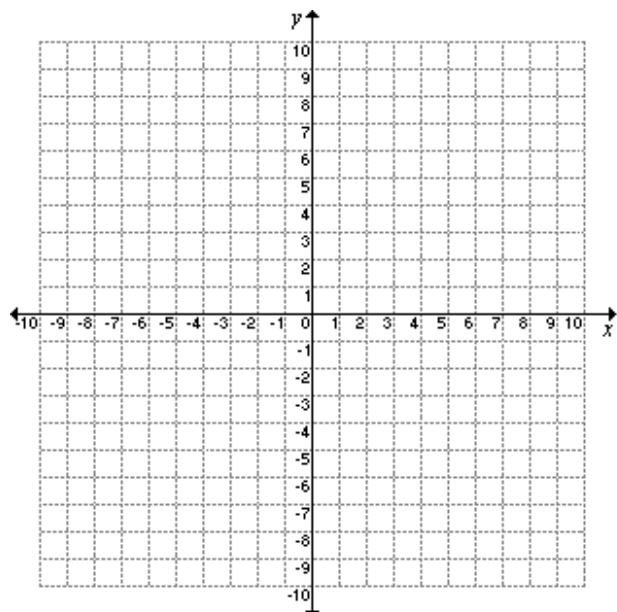
$\{(x, y) \mid y > x, x \in \mathbb{W}, y \in \mathbb{W}\}$



4. Graph each system. Determine a solution for each.

d) $\{(x, y) \mid y - x \geq 3, x \in \mathbb{R}, y \in \mathbb{R}\}$

$\{(x, y) \mid y + 2 \leq x, x \in \mathbb{R}, y \in \mathbb{R}\}$



Linear Inequalities Lesson 2 (With text assignment)

8. Trish is setting up her social networking page:
- She wants to have no more than 500 friends on her new social networking page.
 - She also wants to have at least three school friends for every rugby friend.
 - a) Define the variables and write a system of inequalities that models this situation.
 - b) Describe the restrictions on the domain and range of the variables.
 - c) Graph the solution set to determine two possible combinations of school friends and rugby friends she could have.